

8/19

* look C class notes for global alignment (needleman-wunsch) pseudocode & time complexity

BLOSUM MATRIX

alphabet: $\Sigma = \{A, B, C\}$

observed data: (would be, for instance, protein sequences from related species)

B	A	B	A
A	A	A	C
A	A	C	C
A	A	B	A
A	A	C	C
A	A	B	C

4 columns + 6 rows :

► 6 choose 2 ways to pair amino acids in a column

$$\hookrightarrow \binom{6}{2} * 4 \text{ columns} = 60 \text{ total pairings}$$

► 14 A's, 4 B's, 6 C's (24 total)

$$\hookrightarrow \text{frequency: } A \sim \frac{14}{24}, B \sim \frac{4}{24}, C \sim \frac{6}{24}$$

to calculate this, go through each column of the observed data

and calculate the # of ways to get the desired pair

aligned pairs	observed frequency	expected frequency	log likelihood ratio	rounded log likelihood ratio
$A \rightarrow A$	$\binom{14}{24} \cdot \binom{14}{24} + \binom{10}{24} \cdot \binom{10}{24} / 60 = \frac{28}{60}$	$(\frac{14}{24})(\frac{14}{24}) = \frac{14^2}{24^2}$	$2 \log(\frac{\text{obs}}{\text{exp}}) = 0.7$	1
$A \rightarrow B$	$\frac{5+3}{60} = \frac{8}{60}$	$2(\frac{14}{24})(\frac{4}{24}) = \frac{112}{24^2}$	-1.09	-1
$A \rightarrow C$	$\frac{2+8}{60} = \frac{10}{60}$	$2(\frac{14}{24})(\frac{6}{24}) = \frac{168}{24^2}$	-1.6	-2
$B \rightarrow B$	$\frac{3}{60}$	$(\frac{4}{24})(\frac{4}{24}) = \frac{16}{24^2}$	-1.7	2
$B \rightarrow C$	$\frac{6}{60}$	$2(\frac{4}{24})(\frac{6}{24}) = \frac{48}{24^2}$	0.53	1
$C \rightarrow C$	$\frac{6}{60} = \frac{1}{10}$	$(\frac{6}{24})(\frac{6}{24}) = \frac{36}{24^2}$	1.8	2

can use these values to populate a biologically significant scoring scheme

Likelihood & Heuristic interpretation of "Alignment Score"

$$\text{ex: } X = \text{AACGTTAA} \\ Y = \text{ALGGGTGT}$$

A	A	L	G	-	T	A	A
A	-	C	G	G	T	G	T

4 matches, 2 indels,

2 mismatches

$$\rightarrow \text{probability of alignment} = P_A = p^4 q^1 r^2 \\ \Delta' = \log(P_A) = 4 \log(p) + 2 \log(q) + 2 \log(r) \\ S = \Delta' - 8 \log(k)$$

K is a constant such that $\log(\frac{p}{k}) = 1$

$$\begin{aligned} S &= \Delta' - 8 \log K = 4 \log p + 2 \log q + 2 \log r - 8 \log K \\ &= 4 \log p - 4 \log K + 2 \log q - 2 \log K + 2 \log r - 2 \log K \\ &= 4 \log \left(\frac{p}{K} \right) + 2 \log \left(\frac{q}{K} \right) + 2 \log \left(\frac{r}{K} \right) \\ &= 4 - 2P - 2T \end{aligned}$$

A	1	-1	-2
B	-1	2	1
C	-2	1	2

Thus, to maximize the likelihood of alignment, you have to maximize the alignment score